







MixLLM: Dynamic Routing in Mixed Large Language Models

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1. Motivation

Which one should I choose?





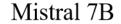
















Llama 3 70B





GPT-3.5 Turbo





GPT-40



Response Quality

We want to select the model which can answer the query correctly.



At the set level, the comparable response quality with lower cost is possible.

Latency

We don't want the query to queue for a long time.

We aim to balance response quality, cost, and latency to achieve the trade-off.

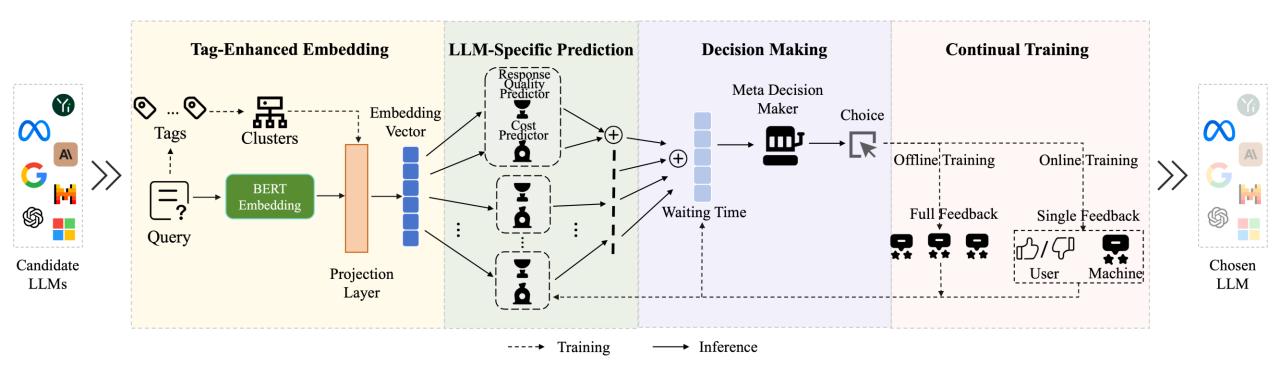


2. Key Challenges & Our Solutions

- Challenge 1: Dynamic trade-offs among quality, cost, and latency.
- Insight: Smart LLM selection reduces cost while maintaining response quality.
- **Solution**: Predict quality and cost and introduce the time penalty to perform query-specific LLM assignments.
- Challenge 2: Enabling continual learning in deployed systems.
- **Insight**: Using feedback improves performance on evolving queries.
- Solution: Real-time learning (user feedback) refines routing choices.
- **Challenge 3**: Navigating a varying set of LLM candidates over time (e.g., new LLM addition or old LLM removal).
- Insight: Dynamically add or remove LLMs without retraining the entire system.
- Solution: The LLM-specific prediction enables plug-and-play integration.



3. MixLLM: Key Components and Workflow

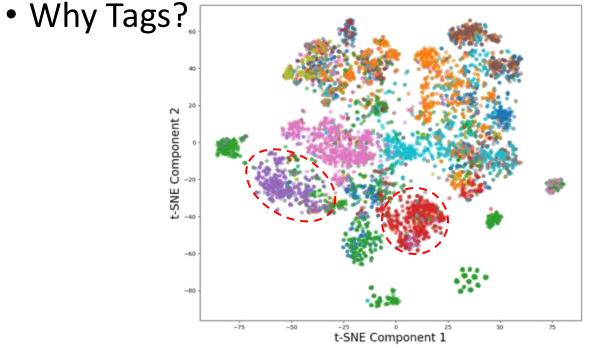


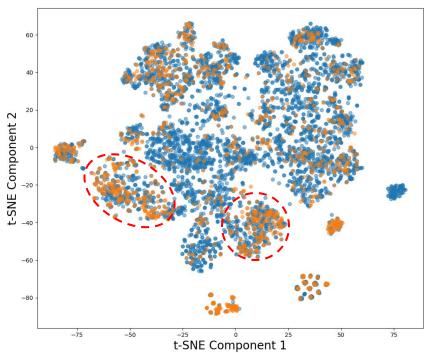
- Informative embedding
- Time penalty

- Individual prediction
- Feedback after depolyment

3.1. Tag-Enhanced Embedding

Generate fine-grained query tags to train the encoder.





Tags have correlation with LLM response quality.



3.1. Tag-Enhanced Embedding

Use BERT-based encoder for sentence embedding:

$$\mathbf{e}_n = \mathsf{Encoder}(q_n),$$

• Employ InsTag [1] to generate **query tags**, then cluster tags into relevant domains.

Train encoder based on these domain clusters:

$$\mathcal{L}_{\text{intra}} = -\frac{1}{|Q|} \sum_{i=1}^{|Q|} \log \frac{\exp(\mathbf{e}_i \cdot \boldsymbol{\mu}_i)}{\sum_{j=1}^{|D|} \exp(\mathbf{e}_i \cdot \boldsymbol{\mu}_j)}.$$

$$\mathcal{L}_{\text{inter}} = \frac{1}{|D|} \sum_{j=1}^{|D|} \log \sum_{k \neq j} \exp(\boldsymbol{\mu}_j \cdot \boldsymbol{\mu}_k).$$

[1] Lu, Keming, et al. "# instag: Instruction tagging for analyzing supervised fine-tuning of large language models." The Twelfth International Conference on Learning Representations. 2023.



3.2. LLM-Specific Prediction

- For each candidate LLM:
 - Predict the **response quality** of this LLM on the current query:

$$\hat{p}_{n,l} = f_l^{\mathsf{rq}}(\mathbf{e}_n; \boldsymbol{\theta}_l^{\mathsf{rq}}),$$

• Predict **response length** to estimate **total cost**:

$$\hat{\mathsf{len}}_{n,l}^{\mathsf{res}} = f_l^{\mathsf{rl}}(\mathbf{e}_n; \boldsymbol{\theta}_l^{\mathsf{rl}}),$$

$$\hat{c}_{n,l} = \underbrace{\mathsf{len}^{\mathsf{prm}}_{n,l} \cdot \mathsf{price}^{\mathsf{prm}}_{l}}_{\text{input cost}} + \underbrace{\mathsf{len}^{\mathsf{res}}_{n,l} \cdot \mathsf{price}^{\mathsf{res}}_{l}}_{\text{output cost}},$$

3.3. Meta Decision Maker

Select the most suitable LLM according to the score:

$$s_{n,l} = s_{n,l}^{\mathsf{trade}} + \alpha \cdot s_{n,l}^{\mathsf{unc}} - \beta \cdot s_{l}^{\mathsf{pen}}.$$

Quality vs. Cost Trade-off: Finds the optimal balance.

$$s_{n,l}^{\mathsf{trade}} = rac{\lambda}{\lambda+1} \cdot \hat{p}_{n,l} - rac{1}{\lambda+1} \cdot \hat{c}_{n,l},$$

• Uncertainty Correction: Adjusts based on confidence in predictions.

$$s_{n,l}^{\mathsf{unc}} = \mathbf{e}_n^T \cdot \mathbf{A}_l^{-1} \cdot \mathbf{e}_n,$$

• Time penalty: Avoids excessive waiting time.

$$s_l^{\mathsf{pen}} = e^{\gamma \cdot (w_l - \xi \cdot \tau)},$$

3.4. Continual Training

Offline Training

- Pre-deployment update
- Full feedback from all candidate LLMs

$$egin{aligned} oldsymbol{ heta}_l^{ ext{rq}} &:= oldsymbol{ heta}_l^{ ext{rq}} - \eta_1 \cdot
abla_{oldsymbol{ heta}_l^{ ext{rq}}} \mathcal{L}(p_{n,l}, \hat{p}_{n,l}), \ oldsymbol{ heta}_l^{ ext{rl}} &:= oldsymbol{ heta}_l^{ ext{rl}} - \eta_2 \cdot
abla_{oldsymbol{ heta}_l^{ ext{rl}}} \mathcal{L}(ext{len}_{n,l}^{ ext{res}}, ext{len}_{n,l}^{ ext{res}}), \ oldsymbol{ heta}_l &:= oldsymbol{ heta}_l + oldsymbol{ heta}_l^T \cdot oldsymbol{ heta}_n. \end{aligned}$$

Online Training

- Post-deployment update
- Partial feedback from the selected LLM
- Binary → Dynamic Feedback Score

$$s'_{n,l} = s_{n,l} + \kappa_{n,l} \cdot s_{n,l}^{\mathsf{df}},$$

$$\left[s_{n,1}^{\mathsf{df}}, s_{n,2}^{\mathsf{df}}, \dots, s_{n,|M|}^{\mathsf{df}}\right] = f^{\mathsf{df}}(\mathbf{e}_n; \boldsymbol{\theta}^{\mathsf{df}}).$$

 Apply the Policy Gradient method to update the parameters.





▼ a MixLLM Demo - a Hugging Fac X +									- 0	9 ×
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MixLLM: Dynamic Routi	ng in Mixed Large Language Models									
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	er to Choose the Best LLM to Answer!	high response latency Given	mived I I Ms with their own st	traneths and weaknesses ITM routing	ng sims to identify the most suitable m	add for each query in the stream	to			
Large Language Models (LLMs) exhibit potential artificial generic intelligence recently, however, their usage is costly with high response latency. Given mixed LLMs with their own strengths and weaknesses. LLM routing aims to identify the most suitable model for each query in the stream to maximize response quality and minimize cost and latency.										
However, the challenges involves (1) dynamic trade-offs among quality, cost, and latency; (2) enabling continual learning in deployed systems; and (3) navigating a varying (e.g., new LLM addition or old LLM removal) set of LLM candidates over time.										
To bridge these gaps, we develop MixLLM, a dynamic contextual-bandit-based routing system for query-LLM assignment. Specifically, we first leverage query tags to enhance query embeddings for the routing task. Next, we design lightweight prediction models to estimate the response qualities and costs of queries over LLMs. We then devise a meta-decision maker to choose the query-LLM assignments to best tradeoff response quality, cost, and latency. Finally, the system benefits from continual training, allowing it to adapt to evolving queries and user feedback over time.										
Our extensive experiments show that MixLLM	Our extensive experiments show that MixLLM achieves the best trade-offs in response quality, cost. and latency (97.25% of GPT-4's quality at 24.18% of the cost under the time constraint).									
🎯 Try MixLLM Routing: E	xperiment with Samples or Your Own Query	y!								
Experience the power of MixLLM's intelligent	routing system by selecting a sample query or inputting your own query. E	explore how MixLLM dynamics	ally assigns queries to the be	est LLM!						
🖈 Try a Sample Query (Qui	ck Demo)		Test Your Own	n Query (Full Routing I	Flow)					
Select a Query			Enter Your Query							
Please select one query		•								
Select Budget			Select Budget							
Very Low			Very Low				•			
	0.0									
	∲ Run Sample				Run Routing					
	✓ Clear Result				✓ Clear Result					
LLM Quali	ty Cost/cent Waiting	ng Time/ms	LLM	Quality	Cost/cent	Waiting Time/ms				
Final Choice	- d : - L L	N /	Final Choice				ء جايد			
MIXLLMIS	a dynamic LL	.M rot	iting	systen	n tnat s	elects	tne			
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How MixLLM Works? Fin	d the Answer in the Following Figure!									

5. Evaluating MixLLM: Performance & Insights

Dataset:

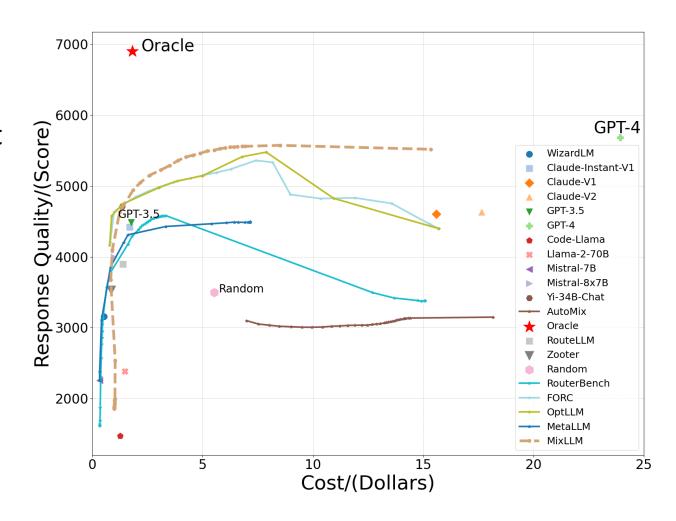
- RouterBench: Consists of 36,497 queries from 8 NLP datasets. Each query is answered by 11 different LLMs.
- Data Split: 80% Training (Offline Training: Pre-train on all LLM responses), 20%
 Testing (Online Training: Adapt using binary feedback)

Baselines:

- AutoMix, RouteLLM, Zooter, RouterBench, FORC, OptLLM, MetaLLM.
- Metric (LLMs cost & latency) source:
 - https://artificialanalysis.ai/

5.1. Overall Routing Performance

- MixLLM:
 - outperforms baselines;
 - achieves 97.25% of GPT-4's quality at 24.18% of the cost under the time constraint;
 - remains stable when the budget is high.
- Why can response quality decline even with a high budget?
 - Higher budgets encourage using powerful LLM, where many queries exceed the waiting time tolerance.



5.2. Study on Continual Training

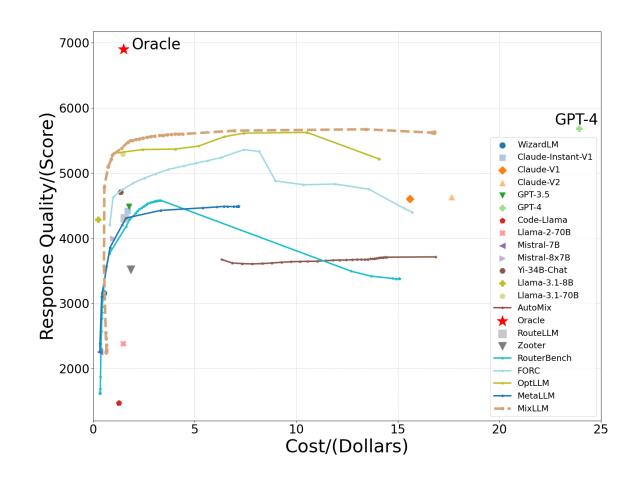
Continual training offers improved performance.

Setting	Offline : Online					
Setting	80:20	50:50	30:70			
Without Online Training	75.54%	71.98%	69.74%			
With Refined Feedback Improvement	76.45% 1.21%	72.99% 1.39%	71.29% 2.22%			
With Binary Feedback Improvement	75.93% 0.52 %	72.37% 0.53 %	70.65% 1.31%			

- In real-world applications, collecting full feedback is **difficult** and **expensive**.
- The responses to queries can serve as partial feedback.
- The amount of data during inference will far exceed that during training.

5.3. Study on Adaptive Training

- We add 2 new models:
 - Llama 3.1 8B;
 - Llama 3.1 70B.
- MixLLM achieves **98.55**% of GPT-4's response quality while reducing the cost to just **18.36**%.
- The original parameters remain unchanged.
 We only train 2 new sets of prediction models.



5.4. Out-of-Domain Generalization

- Real-world queries often originate from new or unseen domains.
- OOD splitting: the test set contains non-overlapping domains not in the training set

Splitting Policy	Offline Only	Offline + Online		
Normal 80:20 Splitting	75.54%	76.45%		
OOD 80:20 Splitting	71.43%	73.89%		
Decrease	5.44%	3.35%		

- The offline-online training strategy effectively enhances domain generalization and adaptation.
- How to solve the OOD routing task?

6. Takeaways & Future Directions

- MixLLM dynamically routes queries to the most suitable LLM while maintaining a balance between response quality, cost, and latency.
- Extensive experiments confirm MixLLM's **effectiveness**: it achieves **97.25**% of GPT-4's quality at only **24.18**% of the cost.
- MixLLM includes **continual training**: it learns from large-scale **post-deployment** data and improves performance over time.
- MixLLM is highly flexible: it can add or remove LLM candidates without requiring full retraining.
- Future work will focus on improving out-of-domain (OOD) generalization and refining LLM selection policies for better performance.









Q & A

Thank you for listening.

Looking forward to collaboration!



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